

## Curriculum Vitae

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### PERSONAL

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Present Status: Professor, Department of Mathematics, ETH Zurich

### EDUCATION

From Sept. 1976 to Oct. 1981 : Ph.D. Program, Combinatorics and Optimization,  
University of Waterloo, Canada  
From April 1976 to August 1976 : Ph.D. Program, Administration Eng., Keio University, Japan  
From April 1974 to March 1976 : Master's Program, Administration Eng., Keio University, Japan  
From April 1970 to March 1974 : Undergraduate, Administration Eng., Keio University, Japan  
From April 1967 to March 1970 : Gakushuuin Highschool, Japan

### DIPLOMAS AND/OR TITLES

May 1999 : Professor Tit., Dept. of Mathematics, ETH Zurich, Switzerland  
September 1982 : Ph.D., Combinatorics and Optimization, University of Waterloo, Canada  
March 1976: M.S., Keio University, Japan  
March 1974: B.S., Keio University, Japan

### RESEARCH FIELDS

Linear, Nonlinear and Combinatorial Optimization, Computational Geometry, Design of Efficient Algorithms, Combinatorics, Oriented Matroid Theory, Combinatorial and Constructive Proof Techniques in Geometry, Development of Computer Software for Geometric and Combinatorial Computation

### PROFESSIONAL ACTIVITIES

1. Referee for J. of Combinatorial Theory (Ser. A and Ser. B), Discrete Mathematics, Combinatorica, Discrete Applied Mathematics, SIAM J. Discrete Mathematics, SIAM J. Computing, Computational and Discrete Mathematics, Mathematical Programming, Mathematics of Operations Research, Discrete and Computational Geometry, European J. of Combinatorics, Graphs and Combinatorics, J. of Operations Research Soc. of Japan, International J. of Mathematics and Mathematical Sciences, European J. of Operational Research, Portugaliae Mathematica, Journal of Graph Theory, etc.
2. Editor for European J. of Combinatorics, Discrete Applied Mathematics (special Issue), Applied Mathematics Research eXpress, Computational Geometry.

3. Ph.D. thesis or Habilitation examiner at University of Tokyo, University of Paris VI, University of Paris Sud, Tokyo Science University, Keio University, Swiss Federal Institute of Technology Lausanne (EPFL) and Zurich (ETHZ), Technical University of Berlin, University of Cantabria, University of Waterloo.
4. Organizer for Franco-Japanese Days on Combinatorics and Optimization (Annual conference started in 1988 by M. Deza and K. Fukuda, held in Tokyo, Paris, Kyoto, Grenoble, Brest, Okinawa), International Symposium on Mathematical Programming 1997 in Lausanne, International Congress of Mathematical Software 2002 (China) and 2006 (Spain), Undercurrent Workshop on Polyhedral Computation in 2003, 2004, FIM Workshop on Geometric Combinatorics 2005 (ETHZ), FIM Workshop on Complexity of Games, Lattice Points and Polyhedra 2006, Summer School: New Algorithmic Paradigms in Optimization 2008.

## GRANTS/DISTINCTIONS/HONORS

2009.4–2012.3	Research Grant, A Fresh Look at the Complexity of Pivoting in Linear Complementarity, Swiss National Science Foundation, Switzerland
2004.10–2007.9	Research Grant, Polytopes, Matroids and Polynomial Systems Swiss National Science Foundation, Switzerland
2002.4–2006.3	Research Grant, Polyhedral Computation, NSERC, Canada
2003.5 –2004	Research Grant, Redundancy Removal in Convex Polyhedra and Its Applications to Optimization and Computational Geometry Swiss National Science Foundation, Switzerland
2000.4–2002.3	Research Grant, Polyhedral Geometry, Enumeration and Computational Complexity, Swiss National Science Foundation, Switzerland
1999.9.23	Editor's Choice Award 1998, Discrete Applied Mathematics for the paper "EP theorems and linear complementarity problems"
1999.5.20	Titular Professor, Swiss Federal Institute of Technology, Switzerland
1999.4	Fellow, Operations Research Society of Japan
1999.2.19–3.5	Visiting Scholar, Wolfram Research Inc., USA
1998.3.6 – 3.14	Invited Professor, Mathematical Institute of Hungarian Academy of Sciences, Budapest, Hungary
1997.10.13 – 10.26	Invited Professor, RIMS, Kyoto University, Kyoto, Japan
1995.10 – 1996.2	Invited Professor, Institute for Mathematical Research, Swiss Federal Institute of Technology, Zurich, Switzerland
1995.1– 1995.10	Invited Professor, Institute for Operations Research, Swiss Federal Institute of Technology, Zurich, Switzerland
1993–1994	Invited Professor, Department of Mathematics, Swiss Federal Institute of Technology, Lausanne, Switzerland
1993	The best paper award, OR Society of Japan for the paper "Linear Complementarity and Oriented Matroids"
1991–1994	Research Grant for New Methods in Combinatorial Optimization, Fujitsu Research Laboratory, Japan
1991–1993	Grant-in-Aids for Co-operative Research, Ministry of Education, Japan
1989–1991	RISE(Research Foundation of Software Engineering, Japan) grant for Franco-Japan joint research
1987–1988	J.S.P.S.(Japan Society for Promotion of Science) / C.N.R.S (France) Joint-Research Fellowship
1984–1989	Grant-in-Aids for Co-operative Research, Ministry of Education, Japan
1976–1981	Canadian Government Scholarship

## PROFESSIONAL CAREER

### Positions Occupied

2008–present	Professor, Department of Mathematics, ETH Zürich
1996–2007	Professor, Department of Mathematics, ETH Zürich and Department of Mathematics, EPF Lausanne
2002–2003	Tenured Professor, School of Computer Science, McGill University, Montreal
1995–1996	Invited Professor, Department of Mathematics, ETH Zürich
1993–1994	Invited Professor, Department of Mathematics, EPF Lausanne
1989–1996	Associate Professor, The University of Tsukuba, Tokyo, Japan
1982–1989	Assistant Professor, Tokyo Institute of Technology, Japan
1978–1981	Teaching Assistant, University of Waterloo, Waterloo, Canada
1974–1976	Teaching Assistant, Keio University, Yokohama, Japan

### Detailed Description of Activities

**January 2008 – present** I work for the institute for Operations Research, ETHZ with a joint appointment (1/3 time) with the group of theoretical computer science headed by Prof. Emo Welzl. In June and July 2008, with Prof. Lüthi and Prof. Welzl, I organized a summer school “New Algorithmic Paradigms in Optimization” in Monte Verita, Ascona.

**October 2003– December 2007** I restarted to work for the institute for Operations Research at ETHZ in joint appointments with two other research groups headed by Prof. Emo Welzl and Prof. Thomas M. Lieblich. I started to coordinate a new Optimization Seminar at ETHZ that is a forum for all researchers interested in the theory and applications of optimization. In collaboration of FIM (the research institute of mathematics of ETHZ), I initiated and coordinated the organization of workshops on discrete mathematics and optimization.

**2002–September 2003** I started to work at the School of Computer Science, McGill University as a tenured full professor in January 2002. The initial activities include teaching of graduate courses on Polyhedral Computation and Information Structures, a core undergraduate course on Algorithms and Data Structures, a coordination of seminars in discrete mathematics and algorithms, and directing a new undergraduate program of software engineering. I created my research lab, Polyhedral Computation Laboratory. Its members include two professors, three doctoral students and three master’s students. I organized the first workshop on polytopes, game and matroids in March 2003 at McGill’s Bellairs Institute.

**1996–2001** In September 1996, I started an ETHZ-EPFL joint project on Optimization and Geometric Computation with T.M. Lieblich, M. Vetterli, H.-J. Lüthi and J. Nievergelt. I was involved in the project since then, and educated several doctoral students in both ETHZ and EPFL. These research activities produced a number of fundamental results and computer codes. Using these we solved many large scale optimization and geometric problems which could not be solved before. Our results have been used in recent software developments in the research group of Günter Ziegler of TU Berlin and are mentioned in the well-known LP-FAQ and Erickson’s WWW page of computational geometry. Also, with a strong collaboration with Emo Welzl (ETHZ), we organized a weekly colloquium on Combinatorics, Geometric Algorithms and Optimization where we exchange new ideas with leading researchers from all over the world. In the fall of 1999, this colloquium became one of the core activities of the European Ph.D. program on Combinatorics, Geometry and Computation, jointly offered by ETH Zurich and three universities in Berlin (Freie Universität, Humboldt-Universität und Technische Universität) together with several leading universities in other European countries. Clearly my research activities shifted toward a highly international research and education for the mutual benefit of the swiss schools and the companion schools. I worked as a thesis advisor for three Ph.D. students, A. Marzetta (ETHZ), A. Andrzejak (ETHZ) and C. Lütolf (EPFL). I supervised three Ph.D. students, L. Finschi (ETHZ), T. Herrmann (ETHZ) and S. Picozzi (EPFL).

My (old) homepage My (old) homepage <http://www.ifor.math.ethz.ch/fukuda/fukuda.html> provides a good account of the activities and the results produced in this period.

**1989–1996** In April 1989, I moved to University of Tsukuba and became associate professor of Graduate School of Systems Management (GSSM). GSSM is the first business school created at a national university in Japan. I taught several courses such as Operations Research, Linear Programming, Combinatorial Optimization, Data Structures and Algorithms and Modern Mathematics with Case Studies. Throughout my Tsukuba years of 1989–96, I visited Europe frequently and worked with researchers in France, Switzerland, Hungary, Germany, Portugal and visiting researchers from North America. In Japan, I started a weekly research seminar on Combinatorics, Geometry and Algorithms. This seminar attracted many young researchers and graduate students from various top universities in Tokyo and its neighborhoods. Ph.D. students I supervised are Keiichi Handa, Antoine Deza and Makoto Namiki.

For the academic year 1993–94, I was invited by Department of Mathematics, EPFL, Lausanne. I carried out joint research with Prof. Thomas M. Liebling, Dr. Prodon and Dr. Francois Margot. Also, I participated in teaching a postgraduate course jointly organized by EPFL and University of Grenoble.

For the period of Jan. 1995 through Sept. 1995, I was invited by Prof. Hans-Jakob Lüthi of ETH Zurich to work for Institute for Operations Research (IFOR) of Mathematics Department. I was then invited by Institute for Mathematical Research (FIM) of ETHZ for the Fall semester 1995 to teach a “nachdiplom” course on Combinatorics of Mathematical Programming. I returned to IFOR in Spring 1996 and continued research there. I organized a colloquium on Optimization and Combinatorics.

**1981–89** In 1981, I accepted an assistant professor position at Department of Information Science, Tokyo Institute of Technology. I took this position in October 1981 and worked through March 1989. I belonged to a decision science group in the department which consists of one full professor, one associate professor and two assistant professors. I mainly worked with a then associate professor, Prof. Masakazu Kojima, to educate students of all levels (undergraduate, master, doctorate) and to carry out research in Optimization Theory, Combinatorics, Algorithms, Complexity Theory and Geometric Computation. I taught undergraduate courses/seminars on Decision Sciences, Linear Programming and Graph Theory. Also, with my initiation, a few assistant professors created a joint seminar on computer science and mathematics, which became the departmental colloquium later. I guided many students to work on linear programming, convex polytopes and computational geometry, combinatorial optimization, enumeration and oriented matroids. In particular, I supervised two Ph.D. students, Akihisa Tamura and Tomomi Matsui. I started several joint research with foreign countries. Among them, Prof. Michel Deza (CNRS, Ecole Normale Supérieure, Paris), Prof. David Avis (McGill University, Montreal) and Prof. Tamas Terlaky (Etvos Lorand University, Budapest and Technical University of Delft). Also, with Prof. Deza we started an annual workshop, Franco-Japanese Days in 1987. The tenth meeting was held in Ecole Polytechnique (France) in September 1997.

**1976–81** Throughout my study for a doctorate degree, I worked as a teaching assistant for several different undergraduate/graduate courses of University of Waterloo, including Calculus, Linear Algebra, Linear Programming. I also taught a undergraduate course on Linear Programming.

**1974–76** During my study for a master’s degree, I worked as a teaching assistant of Keio University in undergraduate mathematics courses. Only a few excellent graduate students were offered a such position.

## LANGUAGES

Mother tongue	: Japanese
Very good knowledge	: English
Good knowledge	:
Elementary knowledge	: French, German

## MAJOR PROFESSIONAL ACHIEVEMENTS

### **Combinatorial Theory of LP and LCP (1992–present)**

In the paper [46] we extended the combinatorial foundation of Linear Programming (LP) to the oriented matroid complementarity theory (OMCP). This can be considered as a simplification of the abstraction

of linear complementarity theory (LCP) developed earlier by M.J. Todd. In particular, we eliminated the heavy machineries to cope with degeneracy which had been standard tools in LCP. We also introduced the notion of duality in LCP and OMCP. Our duality theorem says that every OMCP (LCP) has either a primal complementary solution or a dual complementary solution if the problem is “weakly sufficient.” This theorem includes the LP duality theorem and Cottle’s QP duality theorem as a special case. We gave extremely simple proofs for this theorem, one recursive and one algorithmic (by extending the criss-cross method for Linear Programming), which are both new even when they are specialized to LCP. I received the best paper award of the year 1993 for this paper from the operations research society of Japan.

We have extended the results in [28, 32, 31]. In [32, 24], we have shown the existence of a sequence of admissible pivot operations of polynomial length to an optimal solution. This can be considered as the first step toward a complete answer to the important open question as to whether there exists a *strongly* polynomial algorithm for Linear Programming.

Recently with Kaluzny we have shown a worst-case result [62] for the criss-cross method which says it can visit essentially all bases of an LP.

Two special cases of LCP with P-matrices are investigated in [4, ?] and it was shown that any simple admissible pivot algorithm will solve these cases in strongly polynomial time.

### **Geometric and Computational Combinatorics (1995–present)**

Geometric objects such as convex polytopes, arrangements of hyperplanes and linear programming arise in many disciplines of science. Understanding their discrete structures is often essential in solving optimization or enumeration problems associated with these geometric objects. The theory of oriented matroids lays an ideal foundation for studying the discrete structures underlying geometric objects such as those mentioned. This foundation has been shown to be extremely useful in finding efficient algorithms to solve many basic computational problems over these geometric structures, for example [23, 17, 25, 22, 16, 15]. I gave a graduate lecture on these subjects at ETH Zurich. The lecture notes [90, 88] introduce a new area of research “Geometric and Computational Combinatorics.” My future software development will be based on this foundation which I believe is both theoretically and practically sound.

A recent work on Camion bases can be considered as algorithm study on the simplex regions in arrangements of hyperplanes. New polynomial algorithms to find/recognize Camion bases are proposed in [9].

### **Reverse Search (1992–present)**

In [48], we develop a new pivot algorithm for enumerating all vertices of a convex polyhedron. This algorithm is a substantial improvement over the existing algorithms (e.g. Dyer’s algorithm) since virtually no additional storage is required beyond the input data and the algorithm is more efficient than any previously known algorithms: it finds the  $v$  vertices of a polyhedron in  $R^d$  given by a nondegenerate system of  $n$  inequalities in time  $O(ndv)$ .

The main idea is very simple. Take any objective function on a given polyhedron with a unique optimum vertex. The new algorithm simply starts from the optimum vertex  $v$  and reverse a finite simplex method (e.g. Bland’s rule) in all possible ways. By using the depth-first strategy, this reverse search algorithm finds all vertices without storing the visited vertices.

The same idea can be used to enumerate many interesting objects. In the recent paper [35], we gave various different applications of reverse search scheme, including the enumeration of all triangulations of a finite point set in the plane, that of regions of a hyperplane arrangement in  $R^d$ , etc.

I have been involved in the ZRAM project to develop a parallel implementation reverse search algorithms [27] which was used to solve the largest instances of the vertex enumeration problem. The software library is now freely available.

The more recent applications include the enumeration of  $k$ -sets for a point configuration in  $R^d$  [68], the extended convex hull computation (i.e. facet enumeration of the convex hull of  $k$  H-polytopes in  $R^d$ ) [64],[19], the computation [14, 5, 1] of the Minkowski addition of convex polytopes in  $R^d$ , and the walk in the Gröbner fan of a general polynomial ideal [7, 8].

### **Vertex and Facet Enumeration Codes and Applications** (1984–present)

In 1984, I wrote an open-source code, called PSH (polytope shelling), in Basic to generate all vertices and edges of a 3-dimensional convex polytope, based on my shelling algorithm [82]. I also wrote a 3D visualization program called PGR to polytopes computed by PSH.

In 1988, I started to develop a vertex and facet enumeration code, called pdd, in pascal. It is an implementation of the double description method by Motzkin et al and works quite efficiently for highly degenerate polyhedra.

In 1991, pdd was revised and converted to C. I made this new code cdd publicly available via anonymous ftp [96]. Then, in 1995, I made a C++ version [97] of this code, called cdd+, that runs in exact (rational) arithmetic as well as in usual floating-point arithmetic. The exact version can be used, for example, to prove certain theorems associated with convex polytopes. cdd/cdd+ is considered as one of the most efficient codes for highly degenerate and high dimensional polytopes. Some computational and theoretical results are obtained with this code, for example for cut polytopes in [44] and for analysis of ternary alloys in [41]. A recent effort includes a C-library version [102] of cdd that can be called from C/C++ programs and an interface to Mathematica. As applications, I have written Mathematica notebooks [98] that can be used to draw and build arbitrary polytopes in  $R^3$ .

With I. Mizukoshi, we developed a Mathematica code [101] for the vertex enumeration and made it publicly available by anonymous ftp. This is the first implementation of the reverse search algorithm [48].

### **Enumeration Complexity** (1996–present)

In [79], I introduced a new notion of ENP to classify easy and hard enumeration problems. The classical notions of NP, co-NP, NP-complete, #P etc. are extremely useful but can only deal with the mathematical problems with small output, e.g. the decision problem returns 1 (true) or 0(false). The enumeration problem of listing all qualified objects addresses a much larger class of mathematical problems than the decision problem or the optimization problem. Although there are many open questions to be answered (e.g. what is the completeness in this setting?) I strongly believe the new notion ENP to be proved fundamental in complexity theory.

### **Primal-Dual Algorithm for Vertex and Facet Enumeration** (1996–97)

With D. Bremner and A. Marzetta, we proposed a new algorithmic scheme, primal-dual scheme [30]. This scheme exploits the duality of vertex and facet representations, and it can accelerate existing algorithms when the scheme is incorporated. Most importantly, this algorithm enables us to prove a nice duality: when the vertex (facet) enumeration is polynomially solvable in both input and output sizes for a hereditary class of polytopes, then its converse problem, the facet (vertex) enumeration problem is polynomially solvable.

### **Geometric Computation and Software Developments** (1992–present)

We developed a Mathematica code for unfolding a 3-dimensional convex polytope and made it publicly available by anonymous ftp [94]. There are other Mathematica programs I developed such as the volume computation package for convex polytopes and the triangulation enumeration package.

We have also implemented in C/C++ many existing and new algorithms for volume computation of convex polytopes. This work [26] presents the current best technologies of computing the volume of a high-dimensional convex polytope. The codes are available and used by various researchers worldwide.

An arrangement construction algorithm [23] using reverse search has been implemented to solve maximization of a convex quadratic function over binary variables in parallel. The codes and some of the solved problems with solutions are available at [99, 100] and [12]. It has been adapted to solve basic problems in statistics and geometry, see [61], [11, 10] and [77].

Another problem we have investigated is maximization of the intersection volume of convex polytopes over translation. The paper [6] proposes various efficient algorithms.

The paper [60] proposes an output-sensitive algorithm for the multi-parametric LCP with sufficient matrices.

The international congress of mathematical software (ICMS) headed by Nobuki Takayama addresses a larger framework of mathematical software development where geometric (polyhedral) computation plays an important role, see [84].

### **General Inequalities for Arrangements and Oriented Matroids (1991–98)**

In [49] we proved that in every arrangement of  $n$  hyperplanes in  $R^d$  the mean number of facets of a  $k$ -face is less than  $2k$  for  $k = 1, \dots, d$ . (For simple arrangements, the result can be obtained from Zaslavski's formula for the face number  $f_k$  of  $k$ -faces.) As a corollary, we immediately obtain a nice inequality for the face numbers:  $f_k \leq \binom{d}{k} f_d$  for  $k = 0, \dots, d$ . This result is extended to oriented matroids in [42]. The inequality is used in [50] for efficient enumeration of faces from the full-dimensional faces, and recently in [18] to obtain new results on acyclic orientations of a graph.

### **Connectivity in Oriented Matroids and Zonotopes (1993–98)**

In [45], we proved the connectivities of various graphs associated with oriented matroids. We show that the 1-skeleton of every oriented matroid face poset of rank  $r$  is  $2(r-1)$ , while the 1-skeleton of the polar poset is  $r$ . One of the results implies that the graph (1-skeleton) of every  $d$ -dimensional zonotope is  $2(d-1)$ -connected. The results have been applied to a special case of oriented matroids arising from graphs in [18].

### **Antipodal Graphs and Oriented Matroids (1993)**

In [43], we presented a graph theoretical study of oriented matroids. In particular, we gave a good characterization of oriented matroids of at most rank 3 in terms of tope graphs; a graph  $G$  is isomorphic to the tope graph of an oriented matroid of rank at most 3 if and only if it is planar, antipodal and isometrically embeddable in a hypercube. This result can be considered as an analogue of Steinitz' Theorem characterizing the graphs of 3-polytopes. The paper [43] presents elementary graph operations to construct recursively several classes of graphs arising from oriented matroids and generalizations. This enables us to construct all oriented matroids recursively, for example.

### **General Lower bounds for Convex Polytopes (1994)**

In [40] we proved the best lower bounds for the number of vertices of a general convex  $d$ -polytope with any fixed number of  $k$ -faces. The lower bound for simple polytopes was proved by Barnette, but the general bound was not known for a while. Our bounds are sharp and attained by simplicial  $k$ -neighbourly polytopes.

### **Various Enumeration Algorithms (1992–97)**

I have been working on developing efficient algorithms for various enumeration problems. The papers [47, 39, 36, 37, 33] present algorithms which uses techniques different from the reverse search.

### **Duality in Oriented Matroids (1989–90)**

The papers [56, 54] study the duality of oriented matroids and more general structures. In particular, we characterize the sets  $\mathcal{F}$  of sign vectors satisfying  $(\mathcal{F})^{**} = \mathcal{F}$ , where  $*$  is the orthogonal operator for sign vectors. Various Farkas' type alternative theorems are proved for sign vector systems.

### **Oriented Matroid Deformation Theory (1982–88)**

We developed the local deformation theory of OM. These deformations include perturbation [93], reverse perturbation and flipping operations [58], [80]. These deformations can be used to construct OMs with interesting properties, such as the non-Euclidean property.

### **Oriented Matroid Programming (1982)**

In my Ph.D. thesis [93], I built a combinatorial foundation of LP in the abstract setting of oriented matroids, which became known as the oriented matroid programming (OMP) theory. This includes a simple inductive proof of the duality theorem and simple finite pivot algorithms, all of which are new even when they are restricted to the linear case. This foundation is based on the purely primal treatment of OMP as opposed to the primal-dual treatment of OMP taken by R. Bland in his pioneering work. This primal treatment provides most natural extensions of LP terminologies, and became "standard" as it is employed in the standard oriented matroid book by Björner-Las Vergnas-Sturmfels-White-Ziegler. (This is a joint work with J. Edmonds.)

### **Shellability of Oriented Matroid Polytopes (1982)**

In [93], we proved that every oriented matroid polytope (dual to the Las Vergnas convex set) is shellable. The proof is by extending combinatorially the line shelling technique developed by Bruggesser

and Mani. This shelling is known as the tope graph shelling. The Euler-Poincare relation for an oriented matroid polytope is an immediate corollary. (This is a joint work with J. Edmonds)

### **Non-Euclidean Oriented Matroids and Realizability** (1982)

This is one of the first results in my Ph.D. research [93]. This construction answers positively the question posed by R. Bland which says:

Does there exist an oriented matroid that admits a directed cycle of affine points with respect to a fixed objective element?

When an oriented matroid is linear, such a cycle corresponds to a cyclic sequence of points in an affine  $d$ -space for which a linear function increases monotonically. Thus if such a cycle exists, the matroid must be nonlinear. I did succeed to construct an arrangement of 8 pseudo 2-spheres embedded in the three dimensional unit sphere, which yields an oriented matroid answering the question positively. Such an oriented matroid then became known as non-Euclidean. My example in fact gave birth to the theory of non-Euclidean oriented matroids. Many results on oriented matroids exhibiting a pathological behavior (relative to the linear case) often use some non-Euclidean OM. (A joint work with J. Edmonds and A. Mandel.)

A series of papers have been written on the classification of oriented matroids [2, 3], [75, 76]. One of the main goals there is to decide whether a given oriented matroid is realizable or not, which is a well-known NP-hard problem.

## **LIST OF PUBLICATIONS**

### **(1) Publication in Journals and in Books with Review Board**

- [1] K. Fukuda and C. Weibel. A linear equation for Minkowski sums of polytopes relatively in general position. *Europ. J. Combinatorics*, 31:565–573, 2010. <http://arxiv.org/abs/0712.0027>.
- [2] K. Fukuda, S. Moriyama, and Y. Okamoto. The Holt-Klee condition for oriented matroids. *Europ. J. Combinatorics*, 30(8):1854–1867, 2009. <http://www.arxiv.org/abs/math.CO/0612073>.
- [3] K. Fukuda, S. Moriyama, H. Nakayama, and J. Richter-Gebert. Every non-Euclidean oriented matroid admits a biquadratic final polynomial. *Combinatorica*, 29(6):691–698, 2009. <http://www.arxiv.org/abs/math.CO/0510500>.
- [4] J. Foniok, K. Fukuda, B. Gärtner, and H.-J. Lüthi. Pivoting in linear complementarity: two polynomial-time cases. *Discrete Comput. Geom.*, 42:187–205, 2009. <http://arxiv.org/abs/0807.1249>.
- [5] K. Fukuda and C. Weibel.  $f$ -vectors of Minkowski additions of convex polytopes. *Discrete Comput. Geom.*, 37:503–516, 2007. <http://www.springerlink.com/content/r552751m4081506l/>.
- [6] K. Fukuda and T. Uno. Polynomial time algorithms for maximizing the intersection volume of polytopes. *Pacific Journal of Optimization*, 3:37–52, 2007.
- [7] K. Fukuda, A.N. Jensen, N. Lauritzen, and R. Thomas. The generic Gröbner walk. *J. Symbolic Computation*, 42:298–312, 2007. Electronic version in [http://www.elsevier.com/wps/find/journal\\_browse.cws\\_home](http://www.elsevier.com/wps/find/journal_browse.cws_home).
- [8] K. Fukuda, A. Jensen, and R. Thomas. Computing Gröbner fans. *Mathematics of Computation*, 76:2189–2212, 2007. Electronic version available from <http://www.ams.org/mcom/>.
- [9] K. Fukuda and A. Musitelli. New polynomial-time algorithms for Camion bases. *Discrete Mathematics*, 306:3302–3306, 2006. <http://www.sciencedirect.com/science/journal/>.
- [10] D. Bremner, K. Fukuda, and V. Rosta. Primal-dual algorithms for data depth. In Regina Y. Liu, editor, *Data Depth: Robust Multivariate Analysis, Computational Geometry and Applications*, volume 72 of *DIMACS: Series in Discrete Mathematics and Theoretical Computer Science*, pages 171–194. AMS, 2006.

- [11] K. Fukuda and V. Rosta. Data depth and maximum feasible subsystems. In D. Avis, A. Hertz, and O. Marcotte, editors, *Graph Theory and Combinatorial Optimization*, GERAD's 25th Anniversary Volume, pages 37–67. Springer, 2005.
- [12] J.A. Ferrez, K. Fukuda, and Th. M. Liebling. Solving the fixed rank convex quadratic maximization in binary variables by a parallel zonotope construction algorithm. *European Journal of Operational Research*, 166:35–50, 2005. <http://authors.elsevier.com/sd/article/S0377221704003352>.
- [13] I. Bárány and K. Fukuda. A case when the union of polytopes is convex. *Linear Algebra and its Applications*, 397:381–388, 2005. <ftp://ftp.ifor.math.ethz.ch/pub/fukuda/reports/convuni041108.pdf>.
- [14] K. Fukuda. From the zonotope construction to the Minkowski addition of convex polytopes. *Journal of Symbolic Computation*, 38(4):1261–1272, 2004. pdf file available from <http://www.cs.mcgill.ca/~fukuda/download/paper/minksum031007jsc.pdf>.
- [15] K. Fukuda, S. Onn, and V. Rosta. An adaptive algorithm for vector partitioning. *Journal of Global Optimization*, 25:305–319, 2003. <http://www.cs.mcgill.ca/~fukuda/download/paper/aavp011105.ps.gz>.
- [16] L. Finschi and K. Fukuda. Combinatorial generation of small point configurations and hyperplane arrangements. In B. Aronov and J. Pach, editors, *The Goodman-Pollack Festschrift*, pages 425–440. Springer-Verlag, 2003. <http://www.cs.mcgill.ca/~fukuda/download/paper/cgspc020924.pdf>.
- [17] L. Finschi and K. Fukuda. Generation of oriented matroids – a graph theoretical approach. *Discrete Comput. Geom.*, 27:117–136, 2002. ps file available from <ftp://ftp.ifor.math.ethz.ch/pub/fukuda/reports/GenerationOfOMs001031.ps.gz>.
- [18] K. Fukuda, A. Prodon, and T. Sakuma. Notes on acyclic orientations and the shelling lemma. *Theoretical Computer Science*, 263:9–16, 2001. ps file available from <ftp://ftp.ifor.math.ethz.ch/pub/fukuda/reports/acyclic980112.ps.gz>.
- [19] K. Fukuda, Th. M. Liebling, and C. Lütolf. Extended convex hull. *Computational Geometry*, 20:13–23, 2001. <http://www.sciencedirect.com/science/journal/09257721>.
- [20] A. Deza, K. Fukuda, D. Pasechnik, and M. Sato. On the skeleton of the metric polytope. In J. Akiyama, M. Kano, and M. Urabe, editors, *Lecture Notes in Computer Science*, volume 2098, pages 125–136. Springer-Verlag, 2001.
- [21] A. Bemporad, K. Fukuda, and F.D. Torrisi. Convexity recognition of the union of polyhedra. *Computational Geometry*, 18:141–154, 2001.
- [22] E. Babson, L. Finschi, and K. Fukuda. Cocircuit graphs and efficient orientation reconstruction in oriented matroids. *Europ. J. Combinatorics*, 22(5):587–600, 2001. <http://www.idealibrary.com/links/artid/eujc.2001.0481>.
- [23] K. Allemand, K. Fukuda, Th. M. Liebling, and E. Steiner. A polynomial case of unconstrained zero-one quadratic optimization. *Mathematical Programming, Ser. A*, 91:49–52, 2001.
- [24] K. Fukuda and T. Terlaky. On the existence of a short admissible pivot sequence for feasibility and linear optimization problems. *Pure Mathematics and Applications, Mathematics of Optimization*, 10(4):431–447, 2000. pdf file available at <ftp://ftp.ifor.math.ethz.ch/pub/fukuda/reports/short000214.pdf>.
- [25] R. Cordovil, K. Fukuda, and A. Guedes de Oliveira. On the cocircuit graph of an oriented matroid. *Discrete Comput. Geom.*, 24:257–265, 2000.
- [26] B. Büeler, A. Enge, and K. Fukuda. Exact volume computation for convex polytopes: A practical study. In G. Kalai and G. M. Ziegler, editors, *Polytopes – Combinatorics and Computation*, DMV-Seminar 29, pages 131–154. Birkhäuser, 2000. pdf file available at <http://www.cs.mcgill.ca/~fukuda/download/paper/volcomp980807.pdf> and its implementation <http://www.lix.polytechnique.fr/Labo/Andreas.Enge/Vinci.html>.

- [27] A. Brügger, A. Marzetta, K. Fukuda, and J. Nievergelt. The parallel search bench zram and its applications. *Annals of Operations Research*, 90:45–63, 1999. ps file available from <ftp://ftp.ifor.math.ethz.ch/pub/fukuda/reports/zram970924.ps.gz>.
- [28] K. Fukuda, M. Namiki, and A. Tamura. EP theorems and linear complementarity problems. *Discrete Applied Mathematics*, 84:107–119, 1998.
- [29] I.P.F. Da Silva and K. Fukuda. Isolating points by lines in the plane. *J. Geom.*, 62(1-2):48–65, 1998.
- [30] D. Bremner, K. Fukuda, and A. Marzetta. Primal-dual methods for vertex and facet enumeration. *Discrete Comput. Geom.*, 20:333–357, 1998. ps file available from <ftp://ftp.ifor.math.ethz.ch/pub/fukuda/reports>.
- [31] K. Fukuda and T. Terlaky. Criss-cross methods: A fresh view on pivot algorithms. *Mathematical Programming*, 79:369–395, 1997.
- [32] K. Fukuda, H.-J. Lüthi, and M. Namiki. The existence of a short sequence of admissible pivots to an optimal basis in LP and LCP. *Int. Trans. Opl. Res.*, 4:273–284, 1997.
- [33] K. Fukuda, Th. M. Liebling, and F. Margot. Analysis of backtrack algorithms for listing all vertices and all faces of a convex polyhedron. *Computational Geometry*, 8:1–12, 1997. <http://www.sciencedirect.com/science/journal/09257721>.
- [34] A. Deza, M. Deza, and K. Fukuda. On skeletons, diameters and volumes of metric polyhedra. In M. Deza, R. Euler, and I. Manoussakis, editors, *Combinatorics and Computer Science*, volume 1120 of *Lecture Notes in Computer Science*, pages 112–128. Springer-Verlag, 1996.
- [35] D. Avis and K. Fukuda. Reverse search for enumeration. *Discrete Applied Mathematics*, 65:21–46, 1996.
- [36] K. Fukuda and M. Namiki. Finding all common bases in two matroids. *Discrete Applied Mathematics*, 56:231–243, 1995.
- [37] K. Fukuda and V. Rosta. Combinatorial face enumeration in convex polytopes. *Computational Geometry*, 4:191–198, 1994.
- [38] K. Fukuda and M. Namiki. On extremal behaviors of Murty’s least index method. *Mathematical Programming*, 64:365–370, 1994.
- [39] K. Fukuda and T. Matsui. Finding all the perfect matchings in bipartite graphs. *Appl. Math. Lett.*, 7(1):15–18, 1994.
- [40] A. Deza and K. Fukuda. McMullen’s conditions and some lower bounds for general convex polytopes. *Geometriae Dedicata*, 53:165–173, 1994.
- [41] G. Ceder, G.D. Garbulsky, D. Avis, and K. Fukuda. Ground states of a ternary fcc lattice model with nearest and next-nearest neighbor interactions. *Physical Review B*, 49(1):1–7, 1994. pdf file available from [http://prola.aps.org/abstract/PRB/v49/i1/p1\\_1](http://prola.aps.org/abstract/PRB/v49/i1/p1_1).
- [42] K. Fukuda, A. Tamura, and T. Tokuyama. A theorem on the average number of subfaces in arrangements and oriented matroids. *Geometriae Dedicata*, 47:129–142, 1993.
- [43] K. Fukuda and K. Handa. Antipodal graphs and oriented matroids. *Discrete Mathematics*, 111:245–256, 1993.
- [44] M. Deza, K. Fukuda, and M. Laurent. The inequicut cone. *Discrete Mathematics*, 119:21–48, 1993.
- [45] R. Cordovil and K. Fukuda. Oriented matroids and combinatorial manifolds. *Europ. J. Combinatorics*, 14:9–15, 1993.

- [46] K. Fukuda and T. Terlaky. Linear complementarity and oriented matroids. *Journal of the Operations Research Society of Japan*, 35:45–61, 1992.
- [47] K. Fukuda and T. Matsui. Finding all minimum cost perfect matchings in bipartite graphs. *Networks*, 22:461–468, 1992.
- [48] D. Avis and K. Fukuda. A pivoting algorithm for convex hulls and vertex enumeration of arrangements and polyhedra. *Discrete Comput. Geom.*, 8:295–313, 1992.
- [49] K. Fukuda, S. Saito, A. Tamura, and T. Tokuyama. Bounding the number of  $k$ -faces in arrangements of hyperplanes. *Discrete Applied Mathematics*, 31:151–165, 1991.
- [50] K. Fukuda, S. Saito, and A. Tamura. Combinatorial face enumeration in arrangements and oriented matroids. *Discrete Applied Mathematics*, 31:141–149, 1991.
- [51] K. Fukuda and T. Matsui. On the finiteness of the criss-cross method. *European Journal of Operational Research*, 52:119–124, 1991.
- [52] R. Cordovil, K. Fukuda, and M.L. Moreira. Clutters and matroids. *Discrete Mathematics*, 89:161–171, 1991.
- [53] D. Avis and K. Fukuda. A basis enumeration algorithm for linear systems with geometric applications. *Applied Mathematics Letters*, 4(5):39–42, 1991.
- [54] K. Fukuda and A. Tamura. Dualities in signed vector systems. *Portugaliae Mathematica*, 47:151–165, 1990.
- [55] M. Deza and K. Fukuda. Loops of clutters. In D.K. Ray-Chaudhuri, editor, *Coding Theory and Design Theory, Part I Coding Theory*, volume 20 of *The IMA Volumes in Mathematics and Its Applications*, pages 72–101. Springer-Verlag, 1990.
- [56] K. Fukuda and A. Tamura. Characterizations of  $*$ -families. *J. Combin. Theory Ser. B*, 47:107–110, 1989.
- [57] A. Tamura, H. Takehara, K. Fukuda, S. Fujishige, and M. Kojima. A dual interior point primal simplex method for linear programming. *Journal of the Operations Research Society of Japan*, 31:413–430, 1988.
- [58] K. Fukuda and A. Tamura. Local deformation and orientation transformation in oriented matroids. *Arts Combinatoria*, 25A:243–258, 1988.

## (2) Proceedings with Review Board

- [59] H. Miyata, S. Moriyama, and K. Fukuda. Complete enumeration of small realizable oriented matroids. In *Proceedings of CCCG (Canadian Conference on Computational Geometry)*, 2010.
- [60] S. Columbano, K. Fukuda, and C. Jones. An output-sensitive algorithm for multi-parametric lcps with sufficient matrices. In D. Avis, D. Bremner, and A. Deza, editors, *Polyhedral Computation*, volume 48 of *CRM Proceedings and Lecture Notes*, pages 73–102. Amer. Math. Soc., Providence, RI, 2009. <http://arxiv.org/abs/0807.2318>.
- [61] K. Fukuda and V. Rosta. Exact parallel algorithms for the location depth and the maximum feasible subsystem problems. In C.A. Floudas and P. M. Pardalos, editors, *Frontiers in global optimization*, volume 74 of *Nonconvex Optim. Appl.*, pages 123–133. Kluwer Acad. Publ., Boston, MA, 2004.
- [62] K. Fukuda and B. Kaluzny. The criss-cross method can take  $\omega(n^d)$  pivots. In *Proc. 20th Annu. ACM Sympos. Comput. Geom.*, pages 401–408. ACM Press, New York, 2004. <http://www.acm.org/dl/>.

- [63] D. Avis, K. Fukuda, and S. Picozzi. On canonical representations of convex polyhedra. In A. M. Cohen, X.-S. Gao, and N. Takayama, editors, *Mathematical Software, Proceedings of the First International Congress of Mathematical Software*, pages 350–360. World Scientific Publishing, 2002.
- [64] K. Fukuda, Th. M. Liebling, and C. Lütolf. Extended convex hull. In D. Bremner, editor, *Proceedings of the 12th Canadian Conference on Computational Geometry*, pages 57–63, 2000.
- [65] A. Deza, K. Fukuda, D. Pasechnik, and M. Sato. Generating vertices with symmetries. In *Proc. 5th Workshop on Algorithms and Computation, Tokyo*, pages 1–8, 2000.
- [66] A. Bemporad, K. Fukuda, and F.D. Torrisi. Convexity recognition and computation of the union of polytopes. Technical report AUT00-13, ETH Zurich, ETH Zurich, 2000. presented at International Conference on Advances in Convex Analysis and Global Optimization, Samos, Greece (June 2000).
- [67] L. Finschi, K. Fukuda, and H.-J. Lüthi. Towards a unified framework for randomized pivoting algorithms in linear programming. In P. Kall and H.-J. Lüthi, editors, *Operations Research Proceedings 1998*, pages 113–122, 1999. ps file available from <ftp://ftp.ifor.math.ethz.ch/pub/fukuda/reports/randsimp9810.ps.gz>.
- [68] A. Andrzejak and K. Fukuda. Optimization over k-set polytopes and efficient k-set enumeration. In *Proc. 6th International Workshop on Algorithms And Data Structures (WADS'99)*, LNCS 1663, pages 1–12. Springer-Verlag, 1999.
- [69] J.-A. Ferrez, K. Fukuda, and Th. M. Liebling. Parallel computation of the diameter of a graph. In J. Schaeffer, editor, *High Performance Computing Systems and Applications*, pages 283–296. Kluwer Academic Publishers, 1998.
- [70] D. Bremner, K. Fukuda, and A. Marzetta. Primal-dual methods for vertex and facet enumeration. In *Proc. 13th Annu. ACM Sympos. Comput. Geom.*, pages 49–56, 1997.
- [71] A. Deza, K. Fukuda, and V. Rosta. Wagner’s theorem and combinatorial enumeration of 3-polytopes. *Sūrikaisekikenkyūsho Kōkyūroku*, (872):30–34, 1994. Computational geometry and discrete geometry (Japanese) (Kyoto, 1993).
- [72] D. Avis and K. Fukuda. A pivoting algorithm for convex hulls and vertex enumeration of arrangements and polyhedra. In *Proc. 7th Annu. ACM Sympos. Comput. Geom.*, pages 98–104, 1991.
- [73] K. Fukuda and T. Matsui. Elementary inductive proofs for linear programming. In *Kokyuroku*, volume 680. Research Institute for Mathematical Sciences, Kyoto University, 1989.
- [74] M. Deza and K. Fukuda. On bouquets of matroids and orientations. In *Kokyuroku*, volume 587, pages 110–129. Research Institute for Mathematical Sciences, Kyoto University, 1986.

### **(3) Technical Reports, Articles Submitted**

- [75] K. Fukuda, S. Moriyama, and H. Nakayama. Three pathological rank-4 oriented matroids. Technical report, 2008.
- [76] H. Nakayama, S. Moriyama, and K. Fukuda. Realizations of oriented matroids by polynomial optimization. Technical report, 2007. submitted.
- [77] D. Bremner, K. Fukuda, and V. Rosta. Primal-dual algorithms for data depth. Technical report, ETH Zurich, 2004. [ftp://ftp.ifor.math.ethz.ch/pub/fukuda/reports/primaldual040920\\_TR.pdf](ftp://ftp.ifor.math.ethz.ch/pub/fukuda/reports/primaldual040920_TR.pdf).
- [78] A. Andrzejak and K. Fukuda. Debugging of distributed computations via memory-efficient enumeration of global states. HP labs technical reports, HPL-2002-31, HP Laboratories, February 2002. pdf file available from <http://www.hpl.hp.com/techreports/2002/HPL-2002-31.html>.

- [79] K. Fukuda. Complexity of enumeration - evaluating the hardness of listing objects. presented at ETH Zurich, May 1996, also at International Symposium on Math. Programming 1997, 1996. see WWW page <http://www.ifor.math.ethz.ch/~fukuda/fukuda.html>.
- [80] K. Fukuda and A. Tamura. Local deformation and orientation transformation in oriented matroids II. Research Report B-212, Dept. of Information Sciences, Tokyo Institute of Technology, Tokyo, Japan, 1988.
- [81] K. Fukuda and K. Handa. Perturbation of oriented matroids and acycloids. Research Reports on Information Sciences B-172, Tokyo Institute of Technology, 1985.
- [82] K. Fukuda. An efficient pivot algorithm for finding all edges and vertices of convex polytopes: Shelling algorithm. Research Report B-146, Dept. of Information Sciences, Tokyo Institute of Technology, Tokyo, Japan, 1984.
- [83] K. Fukuda. An efficient pivot algorithm for finding all edges and vertices of convex polytopes: 3-dimensional case. Research Report B-131, Dept. of Information Sciences, Tokyo Institute of Technology, Tokyo, Japan, 1983.

#### **(4) Books, Lecture Notes and Expository Articles**

- [84] K. Fukuda, J. van der Hoeven, M. Joswig, and N. Takayama, editors. *Mathematical Software - ICMS 2010*, volume 6327 of *Lecture Notes in Computer Science*. Springer-Verlag, 2010.
- [85] K. Fukuda. Polyhedral computation FAQ. on line document, Swiss Federal Institute of Technology, Zurich, Switzerland, June 2004. Both html and ps versions available from <http://www.ifor.math.ethz.ch/~fukuda/polyfaq/polyfaq.html>.
- [86] K. Fukuda. Combinatorics of convex polytopes (in Japanese). *Sūrikagaku*, (442):46–55, April 2000.
- [87] K. Fukuda. Lecture notes: Optimization techniques, linear and combinatorial optimization. Technical report, Department of Mathematics, Swiss Federal Institute of Technology, Zurich, 1999. ps file available from <ftp://ftp.ifor.math.ethz.ch/pub/fukuda/sources/a99note.ps.gz>.
- [88] K. Fukuda. Lecture notes: Computational combinatorics. Technical report, Department of Mathematics, Swiss Federal Institute of Technology, Zurich, 1999. ps file available from <ftp://ftp.ifor.math.ethz.ch/pub/fukuda/sources/cc99note.ps.gz>.
- [89] K. Fukuda, T. Matsui, and Y. Matsui. A catalog of enumeration algorithms. Project (in progress), ROSO, Department of Mathematics, EPFL, 1996. WWW page at <http://dmawww.epfl.ch/roso.mosaic/kf/enum/enum.html>.
- [90] K. Fukuda. Lecture notes: A constructive approach to polyhedral geometry and mathematical programming. Institute for Operations Research, ETH, Zurich, Switzerland, 1995.
- [91] K. Fukuda. Reverse search with applications (in Japanese). In S. Fujishige, editor, *Discrete Structures and Algorithms II*, pages 47–78. Kindaikagaku-sha, 1993.
- [92] K. Fukuda. Oriented matroids and linear programming (in Japanese). *Communications of the Operations Research Society of Japan*, (1):5–13, 1987.
- [93] K. Fukuda. *Oriented matroid programming*. Ph.D. thesis, Univ. of Waterloo, Waterloo, Canada, 1982. <ftp://ftp.ifor.math.ethz.ch/pub/fukuda/reports/fukuda1982thesis.pdf>.

## (5) Software

- [94] M. Namiki and K. Fukuda. *UnfoldPolytope: A Mathematica package for unfolding general convex polytopes*, 1992. available from <http://www.ifor.math.ethz.ch/~fukuda/fukuda.html>.
- [95] K. Fukuda and V. Rosta. *Mathematica package for face enumeration*. Graduate School of Systems Management, University of Tsukuba, Tokyo, Japan, 1992. distributed as a supplementary package to VertexEnum package, available via anonymous ftp from cs.sunysb.edu (directory pub/Combinatorica) and from MathSource (Wolfram Research).
- [96] K. Fukuda. *cdd.c : C-implementation of the double description method for computing all vertices and extremal rays of a convex polyhedron given by a system of linear inequalities*. Department of Mathematics, Swiss Federal Institute of Technology, Lausanne, Switzerland, 1993. program available from <http://www.ifor.math.ethz.ch/~fukuda/fukuda.html>.
- [97] K. Fukuda. *cdd+ reference manual*. Institute for Operations Research, Swiss Federal Institute of Technology, Zurich, Switzerland, 1995. program available from <http://www.ifor.math.ethz.ch/~fukuda/fukuda.html>.
- [98] K. Fukuda. Polytope drawing and model building with mathematica and external tools (poly\_cddml.nb and poly\_cddmlgmp.nb). Mathematica notebook, Swiss Federal Institute of Technology, Lausanne and Zurich, 2004. <http://www.cs.mcgill.ca/~fukuda/download/mathematica/Polyhedra/>.
- [99] K. Fukuda and J.A. Ferrez. Implementations of LP-based reverse search algorithms for the zonotope construction and the fixed-rank convex quadratic maximization in binary variables using the zram and the cddlib libraries, 2002. [http://www.cs.mcgill.ca/~fukuda/download/mink/RS\\_TOPE020713.tar.gz](http://www.cs.mcgill.ca/~fukuda/download/mink/RS_TOPE020713.tar.gz).
- [100] J.A. Ferrez, K. Fukuda, and T.M. Liebling. Solutions to random instances of the 01QP obtained by the parallel zonotope construction code rs\_topo.c, 2002. [http://www.cs.mcgill.ca/~fukuda/download/paper/cutzono\\_solutions.tar.gz](http://www.cs.mcgill.ca/~fukuda/download/paper/cutzono_solutions.tar.gz).
- [101] K. Fukuda and I. Mizukoshi. Mathematica package: Vertex enumeration for convex polyhedra and hyperplane arrangements. Technical Report Version 0.41 Beta, Graduate School of Systems Management, University of Tsukuba, Tokyo, Japan, 1991. available via anonymous ftp from cs.sunysb.edu (directory pub/Combinatorica) and from MathSource (Wolfram Research).
- [102] K. Fukuda. cdd, cddplus and cddlib homepage. [http://www.ifor.math.ethz.ch/~fukuda/cdd\\_home/index.html](http://www.ifor.math.ethz.ch/~fukuda/cdd_home/index.html).

## PRESENTATIONS IN RECENT YEARS

- “On the Complexity of Minkowski Sums of Polytopes,” Plenary Talk, Workshop on Combinatorial Geometry and Algorithms, Tokyo Institute of Technology, September 21, 2010.
- “Recent advances in oriented matroids: Interplay between linearity and combinatorics,” Invited Talk, Bernoulli Conference on Discrete & Computational Geometry, EPFL, August 30-September 3, 2010.
- “Toward a Strongly Polynomial Algorithm for the Linear Complementarity Problems with Sufficient Matrices,” Invited Talk, Tokyo Institute of Technology, Tokyo, Japan, January 14, 2009.
- “Exact Algorithms and Software in Optimization and Polyhedral Computation,” Invited Tutorial, International Symposium on Symbolic and Algebraic Computation, Linz, Austria, July 20, 2008.
- “Introduction to polyhedral computation,” EUROPT-OMS Conference on Optimization, Invited Lecture, Prague, Czech Republic, July 5, 2007.
- “On the complexity of Minkowski sums of polytopes,” International Combinatorics, Geometry and Computer Science Conference (CGCS2007), Invited Lecture, Luminy, France, May 3, 2007.

- “Multiparametric LCP, critical regions and sufficient matrices,” Workshop on Advances in Optimization, Tokyo Institute of Technology, Tokyo, Japan, April 20, 2007.
- “Minkowski sums of polytopes relatively in general position,” The 5th Hungarian-Japanese Symposium on Discrete Mathematics and Its Applications, Tohoku University, Sendai, Japan, April 3, 2007.
- “On the Complexity of Minkowski sums of polytopes,” Research Talk, Geometric and Topological Combinatorics, Oberwolfach, Germany February 2007.
- “Introduction to polyhedral computation,” Workshop on Polyhedral Computation, Montreal, invited talk, October 23-26, 2006.
- “Polyhedral computation in algebraic statistics,” invited talk, CMI Workshop: Algebraic Statistics and Computational Biology, the Clay Mathematics Institute, Cambridge, November 12-14, 2005.
- “The Nesterov rounding and perfectly centered polytopes,” invited talk, the joint AMS-DMV-OeMG meeting, Mainz, Germany, June 16-19, 2005.
- “Introduction to the representation conversion for convex polytopes,” Colloquium on Algorithmic Foundations of Bioinformatics, ETH Zurich, Switzerland, March 22, 2005.
- “Generating all vertices in implicitly defined polytopes,” RIMS, Kyoto University, February 17, 2005.
- “Generating all vertices in implicitly defined polytopes,” University of Tokyo, February 10, 2005.
- “The union of convex polytopes: When is it convex? How can one wrap it?” Department of Mathematical and Computing Sciences, Tokyo Institute of Technology, February 9, 2005.
- “Generating all vertices in implicitly defined polyhedra,” Plenary Talk, VOCAL 2004, Veszprém, Hungary, December 14, 2004.
- “Old and new ideas of constructing non-representable oriented matroids,” Research Talk, Geometric Combinatorics, PCMI/IAS, Park City, Utah, July 2004.
- “Drawing and Building Polytopes,” Cross Program in Geometric Combinatorics, PCMI/IAS, Park City, Utah, July 2004.
- “On the connectivity of the flip graph of acyclic orientations,” Seminar, Equipe Combinatoire, University of Paris 6, France, June 2004.
- “Old and new ideas of constructing non-representable oriented matroids,” Seminar, Equipe Combinatoire, University of Paris 6, France, May 2004.
- “From the Zonotope Construction to the Minkowski Addition of Convex Polytopes,” 4th International Conference on Frontiers in Global Optimization, Santorini, June 12, 2003.
- “A parallel implementation of an arrangement construction algorithm,” Invited talk, DIMACS workshop on Implementation of Geometric Algorithms, Rutgers University, December 2002.
- “Recent advances in polyhedral computation,” Invited talk, FOCM workshop on Optimization, University of Minnesota, Minneapolis, August 2002.
- “Towards the limit of exhaustive search,” Invited talk, Latsis Symposium 2001 on Combinatorial Optimization, EPFL, Lausanne, November 2001.
- “Recent progress in polyhedral computation,” Dagstuhl Seminar on Integration of Algebra and Geometry Software Systems, Dagstuhl, Germany, October 2001.
- “Enumeration complexity and geometric computation,” Optimization Seminar, Advances Optimization Laboratory, McMaster University, Hamilton, Canada, Dec. 4, 2000.

- “Mysteries in linear programming,” Department of Mathematics, University of Calgary, Calgary, Canada November 30, 2000.
- “Vertex and facet enumeration for convex polytopes,” Computer Science Seminar, University of Calgary, Calgary, Canada November 29, 2000.
- “Extended Convex Hull,” Algorithm Seminar, School of Computer Science, McGill University, Montreal, Canada, September 6, 2000.
- “Cocircuit Graphs and Efficient Orientation Reconstruction in Oriented Matroids,” Klee - Grünbaum Geometry Festival, Ein Gev, Sea of Galilee, Israel, April 9 - 16, 2000.
- “Every cubical zonotope is uniquely determined by its dual graph,” Workshop on Lattices, Polytopes and Tilings, Mathematisches Forschungsinstitut, Oberwolfach, Germany, Feb. 27 – Mar. 4, 2000.
- “Linear programming techniques for polyhedral computation,” Invited Talk, Berliner Algorithmen Tag, TU-Berlin, Germany, February 18, 2000.
- “Cocircuit graphs and orientation reconstructions in oriented matroids,” Geometrie Combinatoires, CIRM, France, November 8–12, 1999.
- “Orientation reconstruction problems in arrangements and oriented matroids,” Computational Geometry, Dagstuhl Seminar, Germany, March 7 – 13, 1999.
- “On the existence of a short admissible pivot sequence for feasibility and linear optimization problems,” Workshop on Applied and Computational Geometry, Mathematisches Forschungsinstitut, Oberwolfach, Germany, Jan. 28 – Feb. 6, 1999.
- “Enumeration complexity and geometric combinatorics,” Invited Talk, International Conference on Combinatorial Methods in Mathematics, University of Porto, Portugal, July 9, 1998.
- “Acyclic orientations and the shelling lemma,” Invited Talk, Department of Mathematics, University of Porto, Portugal, July 14, 1998.
- “Vertex enumeration for convex polytopes – algorithms and open problems,” Invited Talk, Mathematical Institute of Hungarian Academic of Sciences, Budapest, Hungary, March 12, 1998.
- “Acyclic orientations, totally cyclic orientations and the shelling lemma,” Invited Talk, Eotvos Lorand University, Budapest, Hungary, March 11, 1998.

## TEACHING

- “Integer Programming,” Department of Mathematics (with J. Foniok), ETH Zurich, Spring 2010.
- “Polyhedral Computation,” Department of Mathematics, ETH Zurich, Spring 2009.
- “Joy of Mathematical Thinking Through Optimization,” Graduate School of Business Science, University of Tsukuba, Tokyo, Winter 2009.
- “Optimization Techniques,” Department of Mathematics (with H.-J. Lüthi), ETH Zurich, Fall/Winter 2004–2008.
- “Summer school: New Algorithmic Paradigms in Optimization,”(with H.-J. Lüthi and E. Welzl), ETH Zurich and Monte Verita, Ascona, June 16–July 2, 2008.
- “Seminar — Optimization and Applications,” (with B. Gärtner, , P. Kall, D. Klatté, H.-J. Lüthi and M. Morari), Department of Mathematics, ETH Zurich, 2006–2008.
- “Predoc-Course: Polyhedral Computation,” Optimization Methods in Discrete Geometry, Berlin, May 17–June 2, 2006.

- “Discrete and Algorithmic Geometry,” (with A. Prodon), Graduate Course, EPF Lausanne, Winter 2005, 2007.
- “Seminar — Advanced Topics in Discrete Mathematics: Polytopes,” Department of Mathematics (with E. M. Feichtner), ETH Zurich, Fall-Winter 2004.
- “Algorithms for Polyhedral Computation,” Doctoral Course in Discrete Systems Optimization, École Polytechnique Fédérale de Lausanne, Lausanne, Summer 2004.
- “Data Structures and Algorithms,” Undergraduate Course, COMP-251B, School of Computer Science, McGill University, Winter 2003.
- “Information Structures I,” Graduate Course, COMP-610A, School of Computer Science, McGill University, Fall 2002.
- “Polyhedral Computation,” Graduate Course, M306-760B, School of Computer Science, McGill University, Winter 2002.
- “Chapitres choisis d’algorithmique,” (with Th.M. Liebling and A. Prodon), École Polytechnique Fédérale de Lausanne, Lausanne, Winter 2000.
- “Discrete Geometry,” Department of Computer Science (with J. Richter-Gebert), ETH Zurich, Winter 2000.
- “Computational Combinatorics,” Department of Mathematics, ETH Zurich, Spring-Summer 1999.
- “Optimierungstechniken,” Department of Mathematics (with H.-J. Lüthi), ETH Zurich, Fall-Winter 1998, 1999 and 2000.
- “Colloquium in Combinatorics, Geometric Algorithms and Optimization,” Graduate Seminar (with H.-J. Lüthi, J. Richter-Gebert and E. Welzl), ETH Zurich, Spring-Summer 1999.
- “Colloquium in Combinatorics, Geometric Algorithms and Optimization,” Graduate Seminar (with H.-J. Lüthi, J. Richter-Gebert and E. Welzl), ETH Zurich, Fall-Winter 1998.
- “Colloquium in Operations Research,” Graduate Seminar (with H.-J. Lüthi, J. Richter-Gebert and E. Welzl), ETH Zurich, Spring-Summer 1998.
- “Joint Colloquium in Operations Research and Algorithms – Geometry – Combinatorics,” Graduate Seminar, ETH Zurich, Spring 1997.
- “Méthodes et Applications sur Ordinateur Parallèles,” Cours postgrade, CAPA, École Polytechnique Fédérale de Lausanne, Lausanne, 1997.
- “A Constructive Approach to Polyhedral Geometry and Mathematical Programming,” Graduate Lecture in Mathematics, Department of Mathematics, ETH Zurich, Fall 1995 - Winter 1996.
- “Constructive LP Theory,” Graduate Seminar in Operations Research, Institute for Operations Research, Department of Mathematics, ETH Zurich, Spring 1995.
- “LP, LCP and Oriented Matroids,” Cours postgrade en Recherche Opérationnelle, École Polytechnique Fédérale de Lausanne, Lausanne, and Université Joseph Fourier, Grenoble, January 1995.
- “Linear Algebra,” Graduate School of Systems Management, University of Tsukuba, Tokyo, Spring 1994.
- “Calculus,” Graduate School of Systems Management, University of Tsukuba, Tokyo, Spring 1994.
- “NP easy and LP theory,” Cours postgrade en Recherche Opérationnelle, École Polytechnique Fédérale de Lausanne, Lausanne, May 1994 (with Jack Edmonds).

- “Algorithms and Data Structures,” Graduate School of Systems Management, University of Tsukuba, Tokyo, 1990-1993.
- “Projects in Mathematical Sciences,” Graduate School of Systems Management, University of Tsukuba, Tokyo, 1989-1993.
- “Systems Management Seminar,” Graduate School of Systems Management, University of Tsukuba, Tokyo, 1989-1993.
- “Analysis for Global Environment,” Graduate School of Systems Management, University of Tsukuba, Tokyo, 1989-1991.
- “Mathematica and its Applications,” Graduate School of Systems Management, University of Tsukuba, Tokyo, 1992-1993.
- “Applications of Advanced Softwares,” Graduate School of Systems Management, University of Tsukuba, Tokyo, spring 1993.
- “Networks and Combinatorial Optimization,” Graduate School of Systems Management, University of Tsukuba, Tokyo, winter 1991, 1992, 1993.
- “Discrete Geometry,” Department of Information Sciences, Tokyo Institute of Technology, Tokyo, fall 1992.
- “Matroids, Oriented Matroids and Computational Geometry,” Cours postgrade en Recherche Opérationnelle, École Polytechnique Fédérale de Lausanne, Lausanne, and Université Joseph Fourier, Grenoble, fall 1993.
- “Fundamental Methods in Mathematical Sciences,” Graduate School of Systems Management, University of Tsukuba, Tokyo, 1989-1992.
- “Graphs and Combinatorics,” Graduate School of Systems Management, University of Tsukuba, Tokyo, winter 1990.
- “Data Structures,” Graduate School of Systems Management, University of Tsukuba, Tokyo, winter 1990.
- “Linear Algebra,” Department of Information Sciences, Tokyo Institute of Technology, Tokyo, spring of 1982-1988.
- “Graph Theory,” Department of Information Sciences, Tokyo Institute of Technology, Tokyo, fall of 1987-88.
- “Research Projects in Mathematical Sciences,” Department of Information Sciences, Tokyo Institute of Technology, Tokyo, fall of 1982-1988.
- “Linear Programming,” Department of Combinatorics and Optimization, University of Waterloo, Waterloo, Canada, spring 1981.

## STUDENTS

### Ph.D.

- Antoine Musitelli, Recognition of generalized network matrices, Department of Mathematics, EPF Lausanne (2007).
- Christophe Weibel, Minkowski sums of polytopes: combinatorics and computation, Ph.D. Thesis, Department of Mathematics, EPF Lausanne (2007).

- Lukas Finschi, A graph theoretical approach for reconstruction and generation of oriented matroids, Ph.D. Thesis, Department of Mathematics, ETH Zurich, (2001).
- Christine Lütolf, Modeling and optimizing energy production, Ph.D. Thesis (advisor), Dept. of Mathematics, EPFL, (2001).
- Artur Andrzejak, On  $k$ -sets and their generalizations, Ph.D. Thesis (advisor), Dept. of Computer Sci, ETHZ, (1999).
- Ambros Marzetta, ZRAM: A Library of Parallel Search Algorithms and Its Use in Enumeration and Combinatorial Optimization, Ph.D. Thesis (advisor), Dept. of Computer Sci, ETHZ, (1998).
- Antoine Deza, Cut and metric polytopes, Ph.D. Thesis, University of Paris Sud (1995) and Ph. D. Thesis, Dept. of Information Sciences, Tokyo Institute of Technology, Tokyo, Japan (1996).
- Makoto Namiki, Combinatorial pivot algorithms for LCP, Ph.D. Thesis, Dept. of Information Sciences, Tokyo Institute of Technology, Tokyo, Japan (1996), currently an assistant professor at University of Tokyo.
- Keiichi Handa, Oriented matroids and related structures, Ph.D. Thesis, Dept. of Mathematical Science, Keio University, Yokohama, Japan(1993), currently a researcher at Systems & Software Engineering Lab, Tohsiba Corporation.
- Tomomi Matsui, Structure of Combinatorial Polyhedra, Ph.D. Thesis, Dept. of Information Sciences, Tokyo Institute of Technology, Tokyo, Japan (1991), currently an associate professor at University of Tokyo.
- Akihisa Tamura, Local deformations in oriented matroids, Ph.D. Thesis, Dept. of Information Sciences, Tokyo Institute of Technology, Tokyo, Japan (1989), currently an associate professor at Kyoto University, Kyoto.

### Graduate Students

- David Adjashvili, Doctoral Program, Department of Computer Science, ETH Zurich.
- Lorenz Klaus, Doctoral Program, Department of Computer Science, ETH Zurich.

### Recent Research Projects

- J. Foniok, K. Fukuda. A fresh look at the complexity of pivoting in linear complementarity. Swiss National Science Foundation Research Project, ETH Zurich, May 2009–April 2012.
- E.M. Feichtner, K. Fukuda, P. Parrilo. Polytopes, matroids and polynomial systems – Studies through the fusion of geometric, combinatorial and algebraic algorithms. Swiss National Science Foundation Research Project, ETH Zurich, October 2004–September 2007.
- K. Fukuda, A. Jensen and R. Thomas. Computing state polyhedra of polynomial ideals, ETH Zurich and University of Washington, Seattle, October 2003–2008.
- K. Fukuda and V. Rosta. Computation of Halfspace and Regression Depths, NSERC, Canada, September 2002–2006.
- K. Fukuda. Polyhedral Computation, NSERC, Canada, April 2002–March 2006.
- K. Fukuda, S. Picozzi and Th.M. Lieblich. Research Project on Redundancy Removal in Convex Polyhedra and Its Applications to Optimization and Computational Geometry, Swiss National Foundation, Switzerland, May 2003– 2004.

- K. Fukuda. Research Project on Polyhedral Geometry, Enumeration and Computational Complexity, Swiss National Foundation, Switzerland, April 2000–March 2002.
- D. Avis and K. Fukuda. The complexity of vertex enumeration and convex hull computation. Research in progress, McGill University and ETHZ, 1995–present.
- K. Fukuda, H.-J. Lüthi, and M. Namiki. Combinatorial pivot algorithms for LP and LCP. ETHZ and University of Tokyo, 1995.
- L. Finschi, K. Fukuda, H.-J. Lüthi, and M. Morari. Convex quadratic programming with few discrete variables. Research project, ETHZ, 1999.
- K. Fukuda, T.M. Liebling (EPFL) H.-J. Lüthi (ETHZ) and M. Vetterli (EPFL). ETHZ-EPFL joint research project on Optimization and Geometric Computation. Research in progress, ETHZ and EPFL, 1995–2001.
  - K. Fukuda, T.M. Liebling and C. Lütolf. Extended Convex Hull. EPFL, 1999.
  - K. Fukuda, B. Gärtner and T. Herrmann. Exact LP Solver. ETHZ, 2000–2001.
  - A. Bemporad, K. Fukuda and F.D. Torrisi. Convexity Recognition and Computation of the Union of Polytopes. ETHZ, 1999–2001.
  - A. Andrzejak, K. Fukuda and E. Welzl. Enumeration and complexity of  $k$ -sets and  $k$ -cells. ETHZ, 1998–1999.
  - L. Finschi, K. Fukuda and H.-J. Lüthi. Computational Combinatorics in Linear Subspaces. ETHZ, 1997–2001.
  - K. Fukuda, G. Heche, T.M. Liebling and A. Prodon. Enumeration and optimization of acyclic orientations. EPFL, 1997–1999.
  - J.-A. Ferrez, K. Fukuda and T.M. Liebling. Parallel algorithms for computing the diameter of a graph. EPFL, 1996–1998.
  - A. Andrzejak, K. Fukuda, T.M. Liebling and E. Welzl. Visualization tools for the  $k$ -set problem. ETHZ and EPFL, 1998.
  - K. Allemand, K. Fukuda, T.M. Liebling and A. Prodon. The unconstrained quadratic zero one programming. EPFL, 1998–2001.
  - B. Büeler, A. Enge and K. Fukuda. Comparing exact volume computation methods for  $d$ -dimensional convex polytopes. IFOR, ETHZ, 1995–1998.